# Calorimetric study of alkali-metal decamolybdates

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The enthalpies of formation of the alkali-metal decamolybdates  $(A_2O)_{x/2} \cdot 10MoO_3 \cdot nH_2O$  (A = Li, Na, K, Rb, and Cs) have been determined by solution calorimetry; relations between the thermodynamic quantities obtained, chemical composition and crystal structures are discussed.

#### Introduction

The alkali-metal decamolybdates of ideal formula, A2O. 10MoO<sub>3</sub>·nH<sub>2</sub>O, form a structurally related family.<sup>1</sup> The complete crystal structures of two members of which, A=K, Na, have been determined.<sup>2,3</sup> For both, the framework structure consists of double chains of edge-sharing MoO<sub>6</sub> octahedra linked by common corners which form wide (0.29 nm diameter) tunnels occupied by the alkali metal ion (Fig. 1). In the case of  $K_2O \cdot 10MoO_3 \cdot 5H_2O_2^2$  space group  $PG_3/m$ , only 5/6 of the 6(h) sites are randomly occupied by Mo and it is suggested that 5 H atoms are attached to the oxygens surrounding the vacant Mo site as two OH<sub>2</sub> and one OH group leading to its structural formulation as KMo<sub>5</sub>O<sub>15</sub>(OH)·2H<sub>2</sub>O. The analogous Na compound<sup>3</sup> differs only in detail from the Kdecamolybdate and, as shown below, the lattice parameters of the whole family of the alkali-metal decamolybdate are closely related. For all these compounds the presence of wide onedimensional tunnels suggest that there should be a rich intercalation chemistry and related properties to investigate. There are no published quantitative thermodynamic data available for these compounds and we present the determination of their enthalpies of formation here.



**Fig. 1** The crystal structure of alkali-metal decamolybdate (after B. Krebs and I. Paulat-Böchen, reference 2 in the text).

# Experimental

### Materials

Alkali-metal decamolybdates were prepared by heating acidified  $A_2MoO_4$  solutions.<sup>1,4</sup>  $A_2MoO_4$  solutions were obtained by dissolving the stoichiometric mixture of  $A_2CO_3$ and  $MoO_3$  with water  $(2A^+ + CO_3^{2^-} + MoO_3 \rightarrow 2A^+ + MoO_4^{2^-} + CO_2\uparrow).\dagger$  In the typical preparation of A-deca samples, 20 ml of 0.30 M  $A_2MoO_4$  solution and 30 ml of 0.4 M HNO<sub>3</sub> solution were mixed [degree of acidification of solution  $HNO_3/Mo = 2$ , (molar ratio)], and then heated at 343 K for 2 h with constant stirring. The A-deca samples were formed as precipitates after such treatment. The samples were collected by suction filtration, washed well with distilled water, and airdried for a few days. It was confirmed by X-ray diffraction that the samples were single pure phases. A-deca samples gradually changed from milky white to light blue in the light. Thus, they were stored in the dark to avoid discoloration.

## Structure and chemical composition

The water contents of the samples were determined by TG–DTA with measurements performed on a Mac Science TG-DTA 2010S system from room temperature to 773 K at a heating rate of 10 K min<sup>-1</sup> in air. The alkali-metal and molybdenum contents in the samples were measured with a Hitachi 180–80 automatic absorption spectrometer using the 670.78 nm line for lithium, the 589.00 nm line for sodium, the 766.49 nm line for potassium, the 780.02 nm line for rubidium, the 852.11 nm line for caesium, and the 313.26 nm line for molybdenum. X-Ray diffraction (XRD) patterns of the samples were obtained using a Rigaku RINT 1200M X-ray diffractometer with Cu-K $\alpha$  radiation.

#### **Calorimetric procedure**

The heats of dissolution of the samples were measured using a Tokyo-Riko MMC-5111 multi-microcalorimeter (conduction type twin calorimeter). The heat flux due to the dissolution was converted to a potential and was recorded by computer at a sampling interval of 1 s. The heat was estimated from the peak area appearing on the heat flux curve by comparison with that due to Joule heat. The internal temperature of this calorimeter was adjusted precisely at  $(298.15\pm0.001)$  K and was monitored using a Beckmann's thermometer calibrated with a A $\Sigma\Lambda$  F 25 precision platinum resistance thermometer. More than five measurements were carried out for each sample. The precision of the calorimeter was tested by measuring the dissolution heat of tris(hydroxymethyl)aminomethane (NIST,

 $<sup>\</sup>dagger Na_2 MoO_4$  solution was prepared by dissolving  $Na_2 MoO_4 \cdot 2H_2 O$  in water.

Table 1 Chemical compositions of  $(A_2O)_{x/2} \cdot 10MoO_3 \cdot nH_2O$ 

|                            | Composition <sup>a</sup>   | [n-(x/2)]/x       |
|----------------------------|--|-------------------|
| Li-deca                    | Li <sub>1.6</sub> Mo <sub>10</sub> O <sub>30.8</sub> ·5.27H <sub>2</sub> O | 2.7               |
| Na-deca                    | $Na_{20}Mo_{10}O_{310} \cdot 6.16H_2O$                                     | 2.6               |
| K-deca                     | $K_{18}Mo_{10}O_{308}\cdot4.14H_{2}O$                                      | 1.8               |
| Rb-deca                    | $Rb_{1,7}Mo_{10}O_{30,9}$ ·3.50H <sub>2</sub> O                            | 1.5               |
| Cs-deca                    | $Cs_{1.8}Mo_{10}O_{30.9}$ ·3.23H <sub>2</sub> O                            | 1.3               |
| <sup>a</sup> The errors of | f alkali-metal and water contents are                                      | within 5 and 0.5% |

respectively.

SRM 724a) and was confirmed to be adequate for calorimetric estimation.<sup>‡</sup>

The molar ratios of solute to reactant species were arranged to be very small in order to justify carrying out reactions independently in the same starting medium and, as far as was possible, stoichiometric amounts of reactants were used according to the thermodynamic cycle chosen.§

The samples were sealed in glass ampoules and used in the calorimeter with 25 ml batches of calorimetric reaction medium, which was prepared by dissolving 40 g of  $K_3Fe(CN)_6$  in 1990 ml of 3.00 M KOH aqueous solution.§ Hygroscopic materials, such as ACl, were dried at 473 K in vacuum ( $10^{-3}$  Pa), for 2 h and then sealed in a glass ampoule together with dried air.¶ The mixing heat of water with the calorimetric medium was measured using water, purified by ion exchange, distillation, and degassing just before usage. The standard molar enthalpies of formation of alkali-metal decamolybdates were estimated from the observed dissolution heats by Hess's law of heat summation.

# Results

Table 1 lists the chemical compositions of the A-deca samples prepared. None have exactly the 'ideal' decamolybdate formula for which x=2 and n=5. Other authors<sup>3,7</sup> have reported similar deficiencies in alkali-metal and water contents with retention of the basic structural type. The H<sub>2</sub>O/alkali-metal ratio is clearly related to the size of the metal ion, higher ratios being associated with the smaller Li and Na ions.

The XRD patterns of the A-decamolybdates are shown in Fig. 2 and all the patterns could be satisfactorily indexed. The Na, K and Rb decamolybdates belong to the hexagonal system with a=b>c,  $\gamma=120^{\circ}$ ; for the corresponding Li and Cs compounds there are small monoclinic distortions causing  $a \neq b ~(\neq c)$ ,  $\gamma \neq 120^{\circ}$ . The refined lattice parameters are listed in Table 2. Parameters a and b vary in a complex fashion but c is almost constant over the whole range. The determination

 $About 0.1 \text{ g of tris(hydroxymethyl)aminomethane was dissolved in 20 ml of 0.10 M HCl solution. The enthalpy of reaction was (-245.81±0.26) J g<sup>-1</sup>. This value agreed well with that in the literature.<sup>5,6</sup>$ 

§The molar ratios of solute to reactant species must be very small in order to justify carrying out each reaction independently, rather than consecutively, in the same starting medium. Strictly the maintenance of stoichiometry in the weights of solute used for calorimetric measurements as per the reaction scheme was necessary on both sides of overall reaction equation. Although we attempted to realize these conditions in our work some solutes gave very small heats of solution and very large errors in measured values and thus for such solutes, we used slightly larger masses than those desirable from stoichiometry considerations. The masses used were as follows: A-deca (A: Li, Na, K, Rb and Cs) (0.03 g), MoO<sub>3</sub> (0.03 g), ACl (0.1–0.5 g), 1.0 M HCl (aq) (0.4 g), and H<sub>2</sub>O (0.5 g).

¶When the ampoule, which was sealed in vacuum, was broken for the measurement, a significant step due to vaporization of solution appears in the heat flow curve. The step could not be compensated for even by using the empty ampoule, sealed in vacuum, as the reference. So dried air, which was prepared by passing through a cold trap soaked in liquid  $N_2$ , was used to fill the ampoule after the vacuum drying treatment.



**Fig. 2** XRD patterns of alkali-metal decamolybdates: (A) Li-deca; (B) Na-deca; (C) K-deca; (D) Rb-deca; (E) Cs-deca.

Table 2 Lattice constants of alkali-metal decamolybdates

|   | Crystal<br>system                                 | Space<br>group   | Lattice constants <sup>a</sup>   |
|---|---|--|--|
| Li-deca                                 | Monoclinic  | $P2_1/m$   | a = 1.0613(5), b = 1.0572(5), c = 0.3716(1), y = 120.14(2)   |
| Na-deca<br>K-deca<br>Rb-deca<br>Cs-deca | Hexagonal<br>Hexagonal<br>Hexagonal<br>Monoclinic | $\begin{array}{c} P6_3/m\\ P6_3/m\\ P6_3\\ P2_1 \end{array}$ | a = 1.0644(3), c = 0.3726(1)<br>a = 1.0578(3), c = 0.3731(1)<br>a = 1.0579(3), c = 0.3729(1)<br>a = 1.0655(6), b = 1.0622(6),<br>$c = 0.3721(1), \gamma = 120.08(3)$ |
| aa-c are in                             | $n m$ and $\gamma$ is in $q$                      | degrees.   |  |

of atomic coordinates is now in progress and a full structural discussion will be given in a future publication.

The calorimetric reactions used for the determination of the enthalpies of formation of  $(A_2O)_{x/2}$ ·10MoO<sub>3</sub>·nH<sub>2</sub>O are given in Table 3 together with the average measured heats of reaction and their uncertainties. From these data the enthalpy change,  $\Delta H^\circ$ , for the overall reaction,

$$A_x O_{x/2} \cdot 10 MoO_3 \cdot nH_2O(s) + xHCl \cdot 55.5H_2O(1)$$
  
= xACl(s) + 10MoO\_3(s) + [n + (x/2) + 55.5xH\_2O](1)

was obtained. Combination of the standard enthalpies of formation for the compounds listed in Table 4 with the corresponding values of  $\Delta H^{\circ}$  so obtained enabled the standard enthalpies of formation (at 298.15 K) listed in Table 5 to be determined. The values of  $\Delta_r H^{\circ}$  given there refer to formation of the decamolybdates from the elements in standard states,

$$xA(s) + 10Mo(s) + 1/2[30 + n + (x/2)]O_2(g) + nH_2(g)$$
  
=  $A_xO_{x/2} \cdot 10MoO_3 \cdot nH_2O(s)$ 

Also given in Table 5 are the corresponding enthalpies of formation of the decamolybdates from the constituent oxides,

(

$$x/2)A_{2}O(s) + 10MoO_{3}(s) + nH_{2}O(1)$$
  
= A<sub>x</sub>O<sub>x/2</sub>·10MoO<sub>3</sub>·nH<sub>2</sub>O(s) (1)

For ease of a later comparison, the enthalpies of formation of the alkali-metal molybdates,  $A_2MoO_4(s)$  from the constituent oxides<sup>1</sup> are included in Table 5,

$$A_2O(s) + MoO_3(s) = A_2MoO_4(s)$$
 (2)

| Table 3 | Calorimetric | reaction | scheme | for | $(A_2O)_{x/2}$ | 2·10MoO <sub>3</sub> · <i>n</i> H | $I_2O$ |
|---------|--------------|----------|--------|-----|----------------|-----------------------------------|--------|
|---------|--------------|----------|--------|-----|----------------|-----------------------------------|--------|

| Reaction   | Alkali-metal ion | $\Delta H^{\circ a}/\mathrm{kJ} \mathrm{mol}^{-1}$ |
|--|------------------|--|
| (a) $A_x O_{x/2} \cdot 10 MoO_3 \cdot nH_2O(s) + (20 - x)OH^-(aq) = xA^+(aq) + 10 MoO_4^{2-}(aq) +$                            | Li <sup>+</sup>  | $-766.4 \pm 2.2$                                   |
| $\{[20-x]/2] + n\}H_2O(aq): \Delta H_1$  | Na <sup>+</sup>  | $-696.3 \pm 2.3$                                   |
|  | $\mathbf{K}^+$   | $-710.4 \pm 4.3$                                   |
|  | $Rb^+$           | $-670.7 \pm 4.8$                                   |
|  | Cs <sup>+</sup>  | $-688.4 \pm 2.7$                                   |
| (b) $MoO_3(s) + 2OH^-(aq) = MoO_4^{2-}(aq) + H_2O(aq): \Delta H_2$   |                  | $-85.20 \pm 0.18$                                  |
| (c) $ACl(s) = A^+(aq) + Cl^-(aq)$ : $\Delta H_3$   | Li <sup>+</sup>  | $-38.75 \pm 0.16$                                  |
|  | Na <sup>+</sup>  | $-0.419 \pm 0.040$                                 |
|  | $\mathbf{K}^+$   | $15.02 \pm 0.18$                                   |
|  | Rb <sup>+</sup>  | $14.97 \pm 0.07$                                   |
|  | Cs <sup>+</sup>  | $14.66 \pm 0.10$                                   |
| (d) HCl·55.5H <sub>2</sub> O(1)+OH <sup>-</sup> (aq)=56.5H <sub>2</sub> O(aq)+Cl <sup>-</sup> (aq): $\Delta H_4$               |                  | $-65.85 \pm 0.52$                                  |
| (e) $H_2O(1) = H_2O(aq): \Delta H_5$   |                  | $-0.061 \pm 0.003$                                 |
| (f) $A_x O_{x/2} \cdot 10 MoO_3 \cdot nH_2O(s) + xHCl \cdot 55.5H_2O(1) = xACl(s) + 10 MoO_3(s) + [n + (x/2) + 55.5x]H_2O(1):$ |                  |  |
| $\Delta H_0 \Delta H_0 = \Delta H_1 - 10\Delta H_2 - x\Delta H_3 + x; \ \Delta H_4 - [(n + 1)\Delta H_2 - x\Delta H_3 + x])$   |                  |  |
| $(x/2) + 55.5x$ ]): $\Delta H_5$   |                  | $48.0 \pm 3.0$                                     |
|  | Na               | $32.0 \pm 3.1$                                     |
|  | K <sup>+</sup>   | $2.4 \pm 4.8$                                      |
|  | Rb <sup>+</sup>  | $49.9 \pm 5.2$                                     |
|  | Cs <sup>+</sup>  | $25.0 \pm 3.4$                                     |
| <sup>a</sup> Uncertainties expressed as twice the standard error of the mean.  |                  |  |

**Table 4** Standard molar enthalpies used to determine the standard molar enthalpies of formation of alkali-metal decamolybdates<sup>*a*</sup>

|                               | $\Delta_{\rm f} H^{\rm o}/{\rm kJ}~{\rm mol}^{-1}$ |                   | $\Delta_{\rm f} H^{\rm o}/{\rm kJ}~{\rm mol}^{-1}$ |
|-------------------------------|--|-------------------|--|
| MoO <sub>3</sub>              | -745.2   | NaCl              | -411.1   |
| HCl·55.5H <sub>2</sub> O      | -165.47  | KCl               | -436.7   |
| H <sub>2</sub> O <sup>2</sup> | -285.830   | RbCl              | -430.6   |
| LiCl                          | -408.3   | CsCl              | -442.8   |
| <sup>a</sup> Kagaku binran,   | Maruzen, Tokyo, 1                                  | 975, ch. 8, p. 95 | 53.  |

Table 5 Standard molar enthalpies of formation

| Li                                       | Na   | K                               | Rb  | Cs                           |
|--|--|---------------------------------|---|------------------------------|
| Standard en $-9623 \pm 3$                | thalpies of form $-10022 \pm 3$                | hation (kJ mol<br>$-9383\pm 5$  | $^{-1}$ ) for A-deca<br>-9196±5                                 | $-9157 \pm 3$                |
| Enthalpies of oxides, $\Delta H_{\rm I}$ | of formation of $/(x/2)$ (kJ mol <sup>-1</sup> | $(2/x)(A_2O)_{x/2}$             | 10MoO <sub>3</sub> ∙ <i>n</i> H <sub>2</sub> O                  | (s) from the                 |
| -235<br>Enthalpies c<br>-176             | -391<br>of reaction of ox<br>-307              | -469<br>tides to form A<br>-390 | -544<br>A <sub>2</sub> MoO <sub>4</sub> (s), $\Delta H$<br>-402 | -551<br>$H_{\rm II}$<br>-423 |
|  |  |                                 |   |                              |

## Discussion

The enthalpy of formation data provided in Table 5 show relatively small and irregular variations in the absolute values of  $\Delta_{\rm f} H[(A_2O)_{x/2}\cdot 10{\rm MoO_3}\cdot n{\rm H_2O(s)}]$ . Of more direct chemical significance is the nearly monotonic variation shown for the enthalpies of their formation, from the constituent oxides,

$$A_2O(s) + (2/x)(10MoO_3)(s) + (2/x)nH_2O(1)$$
  
= 2/x{(A\_2O)\_{x/2} · 10MoO\_3 · nH\_2O}(s)

given by  $(2/x) \Delta H_1$ . These changes parallel changes in the enthalpy of formation of the simple molybdates,  $A_2MoO_4(s)$ ,<sup>8</sup> from their constituent oxides, as measured by  $\Delta H_{II}$ . In both cases the increasing exothermicity of the formation of the alkali-metal molybdates and decamolybdates from the alkalimetal oxides, which follows increasing atomic number of the alkali-metal, is a direct consequence of the decreasing stabilities of the alkali-metal oxides, as measured by  $\Delta_f H[A_2O(s)]$ .<sup>8</sup>

The decamolybdate phases are thermodynamically stable (in so far as the entropy changes between solid phases may be presumed to be small) towards decomposition into 
 Table 6
 The site binding energy of the various alkali-metal ions in the decamolybdate framework

| А                         | $\Delta H_{\rm III}/{ m kJ}~{ m mol}^{-1}$                                 |  |
|---------------------------|--|--|
| Li<br>Na<br>K<br>Rb<br>Cs | $ \begin{array}{r} -1091 \\ -1012 \\ -931 \\ -925 \\ -882 \\ \end{array} $ |  |

 $A_2MoO_4(s)$ ,  $MoO_3(s)$  and  $H_2O(1)$  at room temperature, as comparison between corresponding values of  $\Delta H_I$  and  $\Delta H_{II}$ reveals. A measure of the site binding energy of the various alkali metal ions in the decamolybdate framework is given in Table 6 by the enthalpy changes,  $\Delta H_{III}$ , for the reaction,

$$A^{+}(g) + (1/4)O_{2}(g) + (10/x)MoO_{3}(s) + (n/x)H_{2}O(1) + e^{-}(g)$$
  
= (1/x){(A<sub>2</sub>O)<sub>x/2</sub>·10MoO<sub>3</sub>·nH<sub>2</sub>O}(s)

The sequence of ionic binding energies again follows that of ionic size monotonically. A similar trend is found for enthalpies of hydration of the gaseous ions; Li, -519, Na, -406, K, -322, Rb, -301, Cs, -286 kJ mol<sup>-1.9</sup>

The thermochemical data determined here for the decamolybdate phases can be used as a basis for further discussion of the stabilities of species formed in the three-component system  $MoO_3$ - $A_2O$ - $H_2O$ .

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